

# Algorithmics - Core Course for MCA

Number of credits: 4

**Objectives:** At the end of the course, students should be able to appreciate the inherent structure/hardness of a problem and choose an appropriate strategy to solve the problem and design an algorithm that suits the time complexity requirements of the problem.

**Pre-requisites:** Data structures, Discrete mathematical structures

## SYLLABUS

- Analysis of Algorithms:

Asymptotic Notation; Best, worst and average case analysis of algorithms; Solving recurrence relations using substitution method, generating functions, Master's theorem etc. Discussion of problems: Satisfiability(SAT), CNF-SAT, Min-Vertex Cover, Max-Clique, Graph Coloring, NP-Completeness proofs.

Warm-up to complexity analysis: Heap data structure, priority queue application, *Best, worst and average case* analysis of a few sorting algorithms like heap sort, insertion, bubble, selection, counting and radix sort algorithms

- Strategies for problem solving:

- a) **Divide and Conquer strategy:**

Time complexity analysis for Merge Sort and Quick Sort Algorithms,

- b) **Greedy strategy:**

Theoretical foundation of greedy strategy: Matroids Algorithms for solving problems like Knapsack Problem (Fractional), Minimum Spanning Tree problem; Shortest Paths, Job Scheduling, Huffman's code etc along with proofs of correctness and complexity analysis

c) **Dynamic Programming strategy:**

Identify situations in which greedy and divide and conquer strategies may not work. Understanding of optimality principle. Applications to problems like Coinchange, 0/1 and 0/n- Knapsack, Shortest Paths, Optimal Binary Search Tree(OBST), Chained Matrix Multiplication, Traveling Salesperson Problem(TSP) etc.

d) **Backtracking and Branch & Bound strategies:**

State space tree construction, traversal techniques and solving problems like 0/1 and 0/n knapsack, TSP, Applications of Depth First Search: Topological sorting, Finding strongly connected components and game problems.

• Theory of NP-Completeness:

Complexity classes of P, NP, NP-Hard, NP-Complete, Polynomial reductions, Cook's theorem.

**Text books:**

1. Introduction to Algorithms-T.Cormen, C.E.Leiserson, R.L.Rivest,PHI, 1998.
2. Fundamentals of Algorithmics - G.Brassard and P.Bratley, PH, 1995

**Reference books:**

3. Algorithms- R.Johnsonbaugh and M.Schaefer, Pearson, 2004.